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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% LIST OF THEOREMS FOR THE EXAM %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Explanation:
% the number at the end of line = the number of the theorem in the lecture notes
% the sign before the number:
%      *   these theorems are not explicitly included into
%           the exam questions. Anyway, the knowledge is assumed,
%           including the idea of a proof (in case the theorem
%           was proved during the lectures).
%      +   "difficult theorem" included with this status
%           to exam questions
% no sign  "easy theorem" included with this status
%           to exam questions
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%% Chapter V
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description of the convex, balanced and absolutely convex hull % * V.2
generating a locally convex topology using a neighborhood base % + V.3 and V.4
generating topology using a family of seminorms % V.5 and V.10
on the Minkowski functional of a convex neighborhood of zero % + V.8 including V.7
properties of seminorms and Minkowski functionals % V.11
characterization of continuous linear mappings % V.12 and V.13
characterization of continuous linear functionals % V.14
characterization of bounded sets in LCS % * V.15
relationship of continuous and bounded linear mappings % V.16
properties of HLCS of finite dimension % V.17 and V.18
characterization of finite-dimensional HLCS % + V.20
metrizability of LCS % + V.22 including V.21
characterization of normable TVS % V.23
on equivalent metrics on a Fréchet space % * V.25
on absolutely convex hull of a compact set % V.26–V.28
Banach-Steinhaus theorem % V.29
open mapping theorem % + V.30
Hahn-Banach extension theorem and its applications % V.31–V.34
Hahn-Banach separation theorem and its applications % + V.35 and V.36
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%% Chapter VI
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basic properties of abstract weak topologies % * VI.1
dual to an abstract weak topology % VI.3 and VI.4
Mazur theorem % VI.6 and VI.7
boundedness and weak boundedness % + VI.8
weak topology on a subspace % * VI.9
polar calculus % * VI.11
bipolar theorem % VI.12
Goldstine theorem % VI.14
Banach-Alaoglu theorem % + VI.15 and VI.16
reflexivity and weak compactness % VI.17 and VI.18
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%%% Chapter VII

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density of test functions % VII.1

test functions determine measures and locally integrable functions % VII.2

on functions with zero weak derivatives % * VII.3

properties of weak derivatives % VII.4 (proofs of (a),(b))

on the space of test functions % VII.5

characterizations of distributions % VII.6

examples of distributions % * VII.7

on operations on distributions % VII.8

on distributions with zero derivatives % * VII.9

on convergence of distributions % VII.10

Banach-Steinhaus theorem for distributions % * VII.11

on the support of a distribution % + VII.12 (proofs of (a)-(d))

on translates and directional derivatives of test functions % * VII.13

Fubini theorem for distributions % * VII.14

on convolution of a test function and a distribution % + VII.15

on convolution of two distributions % * VII.16 and the preceding constructions

properties of the Schwartz space % VII.17

characterization of tempered distributions % * VII.18

Banach-Steinhaus theorem for tempered distributions % * VII.19

examples of tempered distributions % * VII.20

continuity of operations on the Schwartz space % VII.21

operations with tempered distributions % VII.22

on convergence of tempered distributions % * VII.23

on the Fourier transform on the Schwartz space % VII.24

properties of the Fourier transform of tempered distributions % VII.25

on translates and directional derivatives of Schwartz functions % * VII.26

Fubini theorem for tempered distributions % * VII.27

on convolution of a Schwartz function and a tempered distribution % VII.28 (proofs of (b) and (d)

only)

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%%% Chapter VIII

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Pettis measurability theorem % + VIII.3 including VIII.2 (and its variants VIII.5 and VIII.4)

construction and properties of the Bochner integral % VIII.7

characterization of Bochner integrability % VIII.8

dominated convergence theorem for Bochner integral % VIII.9

on the weak integral % VIII.11

Bochner integral and a bounded operator % VIII.12

definition and properties of Lebesgue-Bochner spaces % + VIII.14

separability of Lebesgue-Bochner spaces % + VIII.15

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%%% Chapter IX

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Krein-Milman theorem % IX.3 including IX.2

Minkowski-Carathéodory theorem % * IX.4

Milman theorem % IX.6

on the barycenter of a measure % * IX.7

integral representation theorem % * IX.8

extreme points of a metrizable compact convex set % * IX.9